Appendix C

Matrix representations

In many of the calculations we use some conventional matrix representations. In this appendix we show the representations of those matrixes. In section 3.1, we have the following matrixes.

$$\eta_{\nu\rho} = \begin{pmatrix} 1 & 0 & 0 & 0\\ 0 & -1 & 0 & 0\\ 0 & 0 & -1 & 0\\ 0 & 0 & 0 & -1 \end{pmatrix}$$
(C.1)

which is the space-time tensor of four dimensions of the Minkowski space.

$$(M_{\mu\nu}) := \begin{pmatrix} 0 & -K_1 & -K_2 & -K_3 \\ K_1 & 0 & J_3 & -J_2 \\ K_2 & -J_3 & 0 & J_1 \\ K_3 & J_2 & -J_1 & 0 \end{pmatrix}$$
(C.2)

where

similarly

$$(M_{\rho\sigma})^{\mu}_{\nu} = i(\eta_{\sigma\nu}\delta^{\mu}_{\rho} - \eta_{\rho\nu}\delta^{\mu}_{\sigma}) \tag{C.4}$$

where δ^{μ}_{ρ} is the kronecker delta

$$\delta^{\mu}_{\rho} = \begin{cases} 1 & \text{if } \mu = \rho \\ 0 & \text{if } \mu \neq \rho \end{cases}$$
(C.5)

C.1 The Gamma Matrixes

$$\gamma^{0} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}, \gamma^{1} = \begin{pmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 \end{pmatrix}$$
(C.6)

$$\gamma^{2} = \begin{pmatrix} 0 & 0 & 0 & -i \\ 0 & 0 & i & 0 \\ 0 & i & 0 & 0 \\ -i & 0 & 0 & 0 \end{pmatrix} \gamma^{3} = \begin{pmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \\ -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{pmatrix}$$
(C.7)

(C.8)

$$\gamma^{5} = i\gamma^{0}\gamma^{1}\gamma^{2}\gamma^{3} \begin{pmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{pmatrix}$$
(C.9)